

# Package: DiceDesign (via r-universe)

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## Contents

DiceDesign-package . . . . .	2
coverage . . . . .	5
discrepancyCriteria . . . . .	6
discrepESE_LHS . . . . .	8
discrepSA_LHS . . . . .	9
dmaxDesign . . . . .	11

factDesign . . . . .	13
faureprimeDesign . . . . .	14
lhsDesign . . . . .	16
maximinESE_LHS . . . . .	17
maximinSA_LHS . . . . .	19
meshRatio . . . . .	21
mindist . . . . .	22
mstCriteria . . . . .	23
nolhDesign . . . . .	24
NOLHdesigns . . . . .	25
nolhdrDesign . . . . .	26
NOLHDRdesigns . . . . .	27
OA131 . . . . .	29
OA131_scrambled . . . . .	30
olhDesign . . . . .	30
phiP . . . . .	32
rss2d . . . . .	33
rss3d . . . . .	35
runif.faure . . . . .	38
scaleDesign . . . . .	39
straussDesign . . . . .	40
unif.test.quantile . . . . .	42
unif.test.statistic . . . . .	43
unscaleDesign . . . . .	44
wspDesign . . . . .	45
xDRDN . . . . .	46

<b>Index</b>	<b>48</b>
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DiceDesign-package      *Designs of Computer Experiments*

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## Description

Space-Filling Designs (SFD) and space-filling criteria (distance-based and uniformity-based).

## Details

This package provides tools to create some specific Space-Filling Design (SFD) and to test their quality:

- Latin Hypercube designs (randomized or centered)
- Strauss SFD and Maximum entropy SFD, WSP designs
- Optimal (low-discrepancy and maximin) Latin Hypercube designs by simulated annealing and genetic algorithms,
- Orthogonal and Nearly Orthogonal Latin Hypercube designs,
- Discrepancies criteria, distance measures,

- Minimal spanning tree criteria,
- Radial scanning statistic

### Note

Part of this work was conducted on 2006-2009 within the frame of the DICE (Deep Inside Computer Experiments) Consortium between ARMINES, Renault, EDF, IRSN, ONERA and TOTAL S.A. (<http://dice.emse.fr/>).

In this package, only Faure's sequence is implemented. Note that the **randtoolbox** package provides the following quasi random sequences: the Sobol sequence, the Halton (hence Van Der Corput) sequence and the Torus sequence (also known as Kronecker sequence). Note also that the **lhs** package provides other types of algorithms to compute optimized LHS.

### Author(s)

J. Franco, D. Dupuy, O. Roustant, P. Kiener, G. Damblin and B. Iooss. Thanks to A. Jourdan for discussions about OA131.

Maintainer: Celine Helbert <[Celine.Helbert@ec-lyon.fr](mailto:Celine.Helbert@ec-lyon.fr)>

### References

- Cioppa T.M., Lucas T.W. (2007). Efficient nearly orthogonal and space-filling Latin hypercubes. *Technometrics* 49, 45-55.
- Damblin G., Couplet M., and Iooss B. (2013). Numerical studies of space filling designs: optimization of Latin Hypercube Samples and subprojection properties, *Journal of Simulation*, 7:276-289, 2013.
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- Owen A.B. (2020), On dropping the first Sobol point, <https://arxiv.org/abs/2008.08051>.
- Roustant O., Franco J., Carraro L., Jourdan A. (2010), A radial scanning statistic for selecting space-filling designs in computer experiments, *MODA-9 proceedings*.
- Santner T.J., Williams B.J. and Notz W.I. (2003) The Design and Analysis of Computer Experiments, *Springer*, 121-161.

**Examples**

```

# *****
# Designs of experiments
# *****

# A maximum entropy design with 20 points in [0,1]^2
p <- dmaxDesign(20,2,0.9,200)
plot(p$design,xlim=c(0,1),ylim=c(0,1))

# Change the dimnames, adjust to range (-10, 10) and round to 2 digits
xDRDN(p, letter = "T", dgts = 2, range = c(-10, 10))

# *****
# Criteria: L2-discrepancy
# *****
dp <- discrepancyCriteria(p$design,type=c('L2','C2'))
# Coverage measure
covp <- coverage(p$design)

# *****
# Criteria: Minimal Spanning Tree
# *****
mstCriteria(p$design,plot2d=TRUE)

# *****
# Radial scanning statistic: Detection of defects of Sobol designs
# *****

# requires randtoolbox package
library(randtoolbox)

# in 2D
rss <- rss2d(design=sobol(n=20, dim=2), lower=c(0,0), upper=c(1,1),
  type="l", col="red")

# in 8D. All pairs of dimensions are tried to detect the worst defect
# (according to the specified goodness-of-fit statistic).
d <- 8
n <- 10*d
rss <- rss2d(design=sobol(n=n, dim=d), lower=rep(0,d), upper=rep(1,d),
  type="l", col="red")

# avoid this defect with scrambling ?
# 1. Faure-Tezuka scrambling (type "?sobol" for more details and options)
rss <- rss2d(design=sobol(n=n, dim=d, scrambling=2), lower=rep(0,d),
  upper=rep(1,d), type="l", col="red")
# 2. Owen scrambling
rss <- rss2d(design=sobol(n=n, dim=d, scrambling=1), lower=rep(0,d),
  upper=rep(1,d), type="l", col="red")

```

---

coverage	<i>Coverage</i>
----------	-----------------

---

**Description**

Compute the coverage measure

**Usage**

coverage(design)

**Arguments**

design      a matrix (or a data.frame) representing the design of experiments representing the design of experiments in the unit cube  $[0,1]^d$ . If this last condition is not fulfilled, a transformation into  $[0,1]^d$  is applied before the computation of the criteria.

**Details**

The coverage criterion is defined by

$$coverage = \frac{1}{\bar{\gamma}} \left[ \frac{1}{n} \sum_{i=1}^n (\gamma_i - \bar{\gamma})^2 \right]^{1/2}$$

where  $\gamma_i$  is the minimal distance between the point  $x_i$  and the other points of the design and  $\bar{\gamma}$  is the mean of the  $\gamma_i$ .

Note that for a regular mesh, cov=0. Then, a small value of cov means that the design is close to a regular grid.

**Value**

A real number equal to the value of the coverage criterion for the design.

**Author(s)**

J. Franco

**References**

Gunzburger M., Burkardt J. (2004) *Uniformity measures for point samples in hypercubes*, <https://people.sc.fsu.edu/~jburkardt/>.

**See Also**

other distance criteria like [meshRatio](#), [phiP](#) and [mindist](#).  
discrepancy measures provided by [discrepancyCriteria](#).

**Examples**

```
dimension <- 2
n <- 40
X <- matrix(runif(n*dimension), n, dimension)
coverage(X)
```

---

discrepancyCriteria    *Discrepancy measure*

---

**Description**

Compute discrepancy criteria.

**Usage**

```
discrepancyCriteria(design, type='all')
```

**Arguments**

design	a matrix (or a data.frame) corresponding to the design of experiments. The discrepancy criteria are computed for a design in the unit cube $[0,1]^d$ . If this condition is not satisfied the design is automatically rescaled.																
type	type of discrepancies (single value or vector) to be computed:																
	<table> <tr> <td>'all'</td> <td>all type of discrepancies (default)</td> </tr> <tr> <td>'C2'</td> <td>centered L2-discrepancy</td> </tr> <tr> <td>'L2'</td> <td>L2-discrepancy</td> </tr> <tr> <td>'L2star'</td> <td>L2star-discrepancy</td> </tr> <tr> <td>'M2'</td> <td>modified L2-discrepancy</td> </tr> <tr> <td>'S2'</td> <td>symmetric L2-discrepancy</td> </tr> <tr> <td>'W2'</td> <td>wrap-around L2-discrepancy</td> </tr> <tr> <td>'Mix2'</td> <td>mixture L2-discrepancy</td> </tr> </table>	'all'	all type of discrepancies (default)	'C2'	centered L2-discrepancy	'L2'	L2-discrepancy	'L2star'	L2star-discrepancy	'M2'	modified L2-discrepancy	'S2'	symmetric L2-discrepancy	'W2'	wrap-around L2-discrepancy	'Mix2'	mixture L2-discrepancy
'all'	all type of discrepancies (default)																
'C2'	centered L2-discrepancy																
'L2'	L2-discrepancy																
'L2star'	L2star-discrepancy																
'M2'	modified L2-discrepancy																
'S2'	symmetric L2-discrepancy																
'W2'	wrap-around L2-discrepancy																
'Mix2'	mixture L2-discrepancy																

**Details**

The discrepancy measures how far a given distribution of points deviates from a perfectly uniform one. Different L2 discrepancies are available in DiceDesign. For example, if we denote by  $Vol(J)$  the volume of a subset  $J$  of  $[0; 1]^d$  and  $A(X; J)$  the number of points of  $X$  falling in  $J$ , the L2 discrepancy is:

$$D_{L2}(X) = \left[ \int_{[0,1]^{2d}} \left( \frac{A(X, J_{a,b})}{n} - Vol(J_{a,b}) \right)^2 dadb \right]^{1/2}$$

where  $a = (a_1; \dots; a_d)'$ ,  $b = (b_1; \dots; b_d)'$  and  $J_{a,b} = [a_1; b_1) \times \dots \times [a_d; b_d)$ . The other L2-discrepancies are defined according to the same principle with different form from the subset  $J$ .

Among all the possibilities, discrepancyCriteria implements only the L2 discrepancies because it can be expressed analytically even for high dimension.

Centered L2-discrepancy is computed using the analytical expression done by Hickernell (1998). The user will refer to Fleming and Manteufel (2005) to have more details about the wrap around discrepancy.

### Value

A list containing the L2-discrepancies of the design.

### Author(s)

J. Franco, D. Dupuy & B. Iooss

### References

Fang K.T, Li R. and Sudjianto A. (2006) Design and Modeling for Computer Experiments, *Chapman & Hall*.

Fang K-T., Liu M-Q., Qin H. and Zhou Y-D. (2018) Theory and application of uniform experimental designs. *Springer*.

Franco J. (2008) Planification d'expériences numérique en phase exploratoire pour la simulation des phénomènes complexes, *PhD thesis, Ecole Nationale Supérieure des Mines de Saint Etienne*.

Hickernell F.J. (1998) A generalized discrepancy and quadrature error bound. *Mathematics of Computation*, **67**, 299-322.

Pleming J.B. and Manteufel R.D. (2005) *Replicated Latin Hypercube Sampling*, 46th Structures, Structural Dynamics & Materials Conference, 16-21 April 2005, Austin (Texas) – AIAA 2005-1819.

### See Also

distance criteria ([coverage](#), [meshRatio](#), [mindist](#) and [phiP](#))

### Examples

```
dimension <- 2
n <- 40
X <- matrix(runif(n*dimension), n, dimension)
discrepancyCriteria(X)
```

---

discrepESE_LHS	<i>Enhanced Stochastic Evolutionary (ESE) algorithm for Latin Hypercube Sample (LHS) optimization via L2-discrepancy criteria</i>
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---

### Description

The objective is to produce low-discrepancy LHS. ESE is a powerful genetic algorithm to produce space-filling designs. It has been adapted here to main discrepancy criteria.

### Usage

```
discrepESE_LHS(design, T0=0.005*discrepancyCriteria(design,type='C2')[[1]],
inner_it=100, J=50, it=2, criterion="C2")
```

### Arguments

design	a matrix (or a data.frame) corresponding to the design of experiments.
T0	The initial temperature of the ESE algorithm
inner_it	The number of iterations for inner loop
J	The number of new proposed LHS inside the inner loop
it	The number of iterations for outer loop
criterion	The criterion to be optimized. One can choose three different L2-discrepancies: the C2 (centered) discrepancy ("C2"), the L2-star discrepancy ("L2star") and the W2 (wrap-around) discrepancy ("W2")

### Details

This function implements a stochastic algorithm (ESE) to produce optimized LHS. It is based on Jin et al works (2005). Here, it has been adapted to some discrepancy criteria taking into account new ideas about the revaluations of discrepancy value after a LHS elementary perturbation (in order to avoid computing all terms in the discrepancy formulas).

### Value

A list containing:

InitialDesign	the starting design
T0	the initial temperature of the ESE algorithm
inner_it	the number of iterations for inner loop
J	the number of new proposed LHS inside the inner loop
it	the number of iterations for outer loop
criterion	the criterion to be optimized
design	the matrix of the final design (low-discrepancy LHS)
critValues	vector of criterion values along the iterations
tempValues	vector of temperature values along the iterations
probaValues	vector of acceptance probability values along the iterations



**Author(s)**

G.Damblin &amp; B. Iooss

**References**

Damblin G., Couplet M., and Iooss B. (2013). Numerical studies of space filling designs: optimization of Latin Hypercube Samples and subprojection properties, *Journal of Simulation*, 7:276-289, 2013.

M. Morris and J. Mitchell (1995) Exploratory designs for computational experiments. *Journal of Statistical Planning and Inference*, 43:381-402.

R. Jin, W. Chen and A. Sudjianto (2005) An efficient algorithm for constructing optimal design of computer experiments. *Journal of Statistical Planning and Inference*, 134:268-287.

**See Also**

Latin Hypercube Sample([lhsDesign](#)), discrepancy criteria([discrepancyCriteria](#)), geometric criterion ([mindistphiP](#)), optimization ([maximinSA\\_LHS](#), [maximinESE\\_LHS](#), [discrepSA\\_LHS](#))

**Examples**

```
## Not run:
dimension <- 2
n <- 10
X <- lhsDesign(n, dimension)$design
Xopt <- discrepESE_LHS(X, T0=0.005*discrepancyCriteria(X, type='C2')[[1]],
                      inner_it=100, J=50, it=2)
plot(Xopt$design)
plot(Xopt$critValues, type="l")

## End(Not run)
```

---

discrepSA\_LHS

---

*Simulated annealing (SA) routine for Latin Hypercube Sample (LHS) optimization via L2-discrepancy criteria*


---

**Description**

The objective is to produce low-discrepancy LHS. SA is an efficient algorithm to produce space-filling designs. It has been adapted here to main discrepancy criteria.

**Usage**

```
discrepSA_LHS(design, T0=10, c=0.95, it=2000, criterion="C2", profile="GEOM", Imax=100)
```

**Arguments**

design	a matrix (or a data.frame) corresponding to the design of experiments
T0	The initial temperature
c	A constant parameter regulating how the temperature goes down
it	The number of iterations
criterion	The criterion to be optimized. One can choose three different L2-discrepancies: the C2 (centered) discrepancy ("C2"), the L2-star discrepancy ("L2star") and the W2 (wrap-around) discrepancy ("W2")
profile	The temperature down-profile, purely geometric called "GEOM", geometrical according to the Morris algorithm called "GEOM_MORRIS" or purely linear called "LINEAR"
Imax	A parameter given only if you choose the Morris down-profile. It adjusts the number of iterations without improvement before a new elementary perturbation

**Details**

This function implements a classical routine to produce optimized LHS. It is based on the work of Morris and Mitchell (1995). They have proposed a SA version for LHS optimization according to mindist criterion. Here, it has been adapted to some discrepancy criteria taking in account new ideas about the reevaluations of a discrepancy value after a LHS elementary perturbation (in order to avoid computing all terms in the discrepancy formulas).

**Value**

A list containing:

InitialDesign	the starting design
T0	the initial temperature of the SA algorithm
c	the constant parameter regulating how the temperature goes down
it	the number of iterations
criterion	the criterion to be optimized
profile	the temperature down-profile
Imax	The parameter given in the Morris down-profile
design	the matrix of the final design (low-discrepancy LHS)
critValues	vector of criterion values along the iterations
tempValues	vector of temperature values along the iterations
probaValues	vector of acceptance probability values along the iterations

**Author(s)**

G. Damblin & B. Iooss

## References

Damblin G., Couplet M., and Iooss B. (2013). Numerical studies of space filling designs: optimization of Latin Hypercube Samples and subprojection properties, *Journal of Simulation*, 7:276-289, 2013.

M. Morris and J. Mitchell (1995) Exploratory designs for computational experiments. *Journal of Statistical Planning and Inference*, 43:381-402.

R. Jin, W. Chen and A. Sudjianto (2005) An efficient algorithm for constructing optimal design of computer experiments. *Journal of Statistical Planning and Inference*, 134:268-287.

## See Also

Latin Hypercube Sample([lhsDesign](#)), discrepancy criteria([discrepancyCriteria](#)), geometric criterion ([mindistphiP](#)), optimization ([maximinSA\\_LHS](#),[maximinESE\\_LHS](#) ,[discrepESE\\_LHS](#))

## Examples

```
dimension <- 2
n <- 10
X <- lhsDesign(n, dimension)$design

## Optimize the LHS with C2 criterion
Xopt <- discrepSA_LHS(X, T0=10, c=0.99, it=2000, criterion="C2")
plot(Xopt$design)
plot(Xopt$critValues, type="l")

## Optimize the LHS with C2 criterion and GEOM_MORRIS profile
## Not run:
Xopt2 <- discrepSA_LHS(X, T0=10, c=0.99, it=1000, criterion="C2", profile="GEOM_MORRIS")
plot(Xopt2$design)

## End(Not run)
```

---

dmaxDesign

*Maximum Entropy Designs*


---

## Description

Space-Filling Designs with  $n$  experiments based on covariance matrix in  $[0,1]^d$ .

## Usage

```
dmaxDesign(n, dimension, range, niter_max=1000, seed=NULL)
```

**Arguments**

n	number of experiments
dimension	number of variables
range	range of variogram
niter_max	number of iterations
seed	seed used to generate uniform design

**Details**

Maximum entropy design is a kind of optimal design based on Shannon's definition of entropy as the amount of information. Originally, maximum entropy sampling was proposed by Shewry and Wynn (1987). The goal of the design is to maximize the entropy defined as the determinant of the correlation matrix using a Fedorov-Mitchell exchange algorithm.

The spatial correlation matrix is defined by  $C = (\rho_{ij})$ :

$$\rho_{ij} = \begin{cases} 1 - \gamma(h_{ij}) & \text{if } h_{ij} \leq a, \\ 0 & \text{if } h_{ij} > a, \end{cases}$$

where  $h_{ij}$  is the distance between  $x_i$  and  $x_j$ ,  $a$  denotes the range of the variogram and  $\gamma$  is a spherical variogram:

$$\gamma(h) = 1.5 \frac{h}{a} - 0.5 \left( \frac{h}{a} \right)^3 \text{ for } h \leq a$$

**Value**

A list with components:

n	the number of points
design	the design of experiments
dimension	the number of variables
range	the range of the variogram
niter_mx	the number of iterations
design_init	the initial distribution
det_init	the value of the determinant for the initial distribution
det_end	the value of the determinant at the end of the procedure
seed	the value of the seed

**Author(s)**

J. Franco

## References

Currin C., Mitchell T., Morris M. and Ylvisaker D. (1991) *Bayesian Prediction of Deterministic Functions With Applications to the Design and Analysis of Computer Experiments*, American Statistical Association, **86**, 416, 953-963.

Shewry, M. C. and Wynn and H. P. (1987) *Maximum entropy sampling*, Journal of Applied Statistics 14, 165-170.

## Examples

```
n <- 20
dimension <- 2
range <- 0.9
niter_max <- 200
out <- dmaxDesign(n, dimension, range, niter_max)

## Change the dimnames, adjust to range (-10, 10) and round to 2 digits
xDRDN(out, letter = "T", dgts = 2, range = c(-10, 10))
```

---

factDesign

*Full Factorial Designs*

---

## Description

Create a factorial design with  $n = \text{pow}(\text{levels}, \text{dimension})$  experiments in  $[0,1]^d$ .

## Usage

```
factDesign(dimension, levels)
```

## Arguments

dimension	an integer given the number of input variables
levels	an integer given the number of levels

## Details

It is possible to take a different number of levels for any factor. In this case, the argument levels should be a vector.

## Value

factDesign returns a list containing all the input arguments detailed before, plus the following components:

n	the number of experiments
design	the design of experiments

**Author(s)**

G. Pujol and J. Franco

**Examples**

```
## First example
g1 <- factDesign(2, 7)
plot(g1$design, xlim=c(0,1), ylim=c(0,1))

## Second example
g2 <- factDesign(2, c(2,7))
plot(g2$design, xlim=c(0,1), ylim=c(0,1))

## Change the dimnames, adjust to range (-10, 10) and round to 2 digits
xDRDN(g1, letter = "T", dgts = 2, range = c(-10, 10))
xDRDN(g2, letter = "T", dgts = 2, range = c(-10, 10))
```

faureprimeDesign

*A special case of the low discrepancy Faure sequence***Description**

Generate a Faure sequence with  $n = p^u - 1$  experiments in  $[0,1]^d$  or other domains (see the details) where  $p$  is the first prime number equal or larger than  $d$  and  $u$  is an exponent, usually 2.

**Usage**

```
faureprimeDesign(dimension, u = 2, range = c(0, -1))
```

**Arguments**

dimension	the number of variables (< 199)
u	the exponent applied to the prime number
range	the scale (min and max) of the inputs. See the details for the six predefined ranges.

**Details**

This is a special case of `runif.faure` where the number of generated points depends exclusively on the dimension and the selected exponent. For the exponent  $u = 2$ , the design is orthogonal and has resolution 4. It is a perfect grid  $(p - 1)(p + 1)$  on each pair of variables where  $p$  is the first prime number equal or larger than the dimension  $d$ .

Six domain ranges are predefined and cover most applications:

- $c(0, 0)$  corresponds to  $[0, n]^d$ .
- $c(1, 1)$  corresponds to  $[1 - n, n - 1]^d = [2 - p^u, p^u - 2]^d$ .
- $c(0, 1)$  corresponds to  $[0, 1]^d$ .

- $c(0, -1)$  corresponds to  $[p^{-u}, 1 - p^{-u}]^d$ .
- $c(-1, -1)$  corresponds to  $[-1 + 2p^{-u}, 1 - 2p^{-u}]^d$ .
- $c(-1, 1)$  corresponds to  $[-1, 1]^d$ .

### Value

faureprimeDesign returns a list with the following components:

- design: the design of experiments
- n: the number of experiments
- dimension: the dimension
- prime: the prime number
- u: the exponent

### Author(s)

P. Kiener

### References

Faure H. (1982), Discrepance de suites associees a un systeme de numeration (en dimension s), *Acta Arith.*, 41, 337-351.

Owen A.B. (2020), On dropping the first Sobol point, <https://arxiv.org/abs/2008.08051>.

### Examples

```
## Range c(0,-1) returns the design produced by runif.faure()
plan1 <- runif.faure(n = 24, dimension = 5)$design ; plan1
plan2 <- faureprimeDesign(dimension = 5, range = c(0,-1))$design ; plan2
all.equal(plan1, plan2, tolerance = 1e-15)

## Range c(0,0) returns the original sequence of integers.
## The first (p-1) lines are on the first diagonal.
## The remaining lines are LHSs grouped in p-1 blocks of p rows.
d <- p <- 5
plan <- faureprimeDesign(dimension = d, range = c(0,0))$design ; plan
apply(plan, 2, sort)

## A regular grid (p-1)x(p+1) rotated by a small angle
pairs(plan)

plot(plan[,1], plan[,2], las = 1)
points(plan[1:(p-1),1], plan[1:(p-1),2], pch = 17, cex = 1.6)
abline(v = plan[1:(p-1),1], col = 4)

## Designs of dimensions 24x5 in various ranges
lstrg <- list(p0p0 = c(0,0), p1p1 = c(1,1), p0p1 = c(0,1),
             p0m1 = c(0,-1), m1m1 = c(-1,-1), m1p1 = c(-1,1))
lst <- lapply(lstrg, function(rg) faureprimeDesign(
```

```

        dimension = 5, u = 2, range = rg)$design)
lapply(lst, tail)
sapply(lst, range)

## The odd designs (p1m1, m1m1, m1p1) are orthogonal and have resolution 4.
library(lattice)

mat <- lst$m1m1 ; colnames(mat) <- LETTERS[1:5]
fm1 <- ~ (A+B+C+D+E)^2+I(A^2)+I(B^2)+I(C^2)+I(D^2)+I(E^2)
mmm <- model.matrix(fm1, data = as.data.frame(mat))[, -1] ; tail(mmm)
cmm <- round(cov2cor(crossprod(mmm)), 3) ; cmm
lattice::levelplot(cmm[, ncol(cmm):1], at = seq(-1, 1, length.out = 10),
                  col.regions = rev(grDevices::hcl.colors(9, "PuOr")))

```

---

lhsDesign

*Latin Hypercube Designs*


---

### Description

Simple (random) Latin Hypercube Design (randomized or centered) with  $n$  experiments in  $[0,1]^d$ .

### Usage

```
lhsDesign(n, dimension, randomized=TRUE, seed=NULL)
```

### Arguments

n	number of experiments
dimension	number of variables
randomized	TRUE for randomized LHS; FALSE for centered LHS
seed	seed used to generate the random permutations and perturbations

### Details

This program builds a Latin Hypercube Design (LHD), also called a Latin Hypercube Sample (LHS), on the space  $[0,1]^d$  (with uniform probability measures). LHD aims at ensuring that each variable has its whole range well scanned: the range of each variable is divided into  $n$  equally probable stratas. Each stratum of each variable contains only one point of the LHD. Centered LHD is obtained by choosing for each point the center of the corresponding case, while randomized LHD is obtained by adding random perturbations inside each point case.

Once the sample is generated, the uniform sample from a column can be transformed to any distribution by using the quantile functions.



**Value**

A list with components:

n	the number of points
dimension	the number of variables
design	the design of experiments
randomized	the type of LHD
seed	the value of the seed

**Author(s)**

B. Iooss

**References**

McKay M., Conover W. and Beckman R. (1979) *A comparison of three methods for selecting values of input variables in the analysis of output from a computer code*, *Technometrics*, **21**, 2, 239-245.

Stein M. (1987) *Large sample properties of simulations using Latin hypercube sampling*, *Technometrics*, **29**, 143-151.

**See Also**

LHD optimization ([maximinSA\\_LHS](#),[discrepSA\\_LHS](#),[maximinESE\\_LHS](#) ,[discrepESE\\_LHS](#))

**Examples**

```
n <- 20
dimension <- 2
out <- lhsDesign(n, dimension)
out$design

## Change the dimnames, adjust to range (-10, 10) and round to 2 digits
xDRDN(out, letter = "T", dgts = 2, range = c(-10, 10))
```

---

maximinESE_LHS	<i>Enhanced Stochastic Evolutionnary (ESE) algorithm for Latin Hypercube Sample (LHS) optimization via phiP criteria</i>
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**Description**

The objective is to produce maximin LHS. ESE is a powerful genetic algorithm allowing to produce space-filling designs.

**Usage**

```
maximinESE_LHS(design, T0=0.005*phiP(design,p=50), inner_it=100, J=50, it=1, p=50)
```

**Arguments**

design	a matrix (or a data.frame) corresponding to the design of experiments.
T0	The initial temperature of the ESE algorithm
inner_it	The number of iterations for inner loop
J	The number of new proposed LHS inside the inner loop
it	The number of iterations for outer loop
p	power required in phiP criterion

**Details**

This function implements a stochastic algorithm (ESE) to produce optimized LHS. It is based on Jin et al works (2005).

**Value**

A list containing:

InitialDesign	the starting design
T0	the initial temperature of the ESE algorithm
inner_it	the number of iterations for inner loop
J	the number of new proposed LHS inside the inner loop
it	the number of iterations for outer loop
p	power required in phiP criterion
design	the matrix of the final design (maximin LHS)
critValues	vector of criterion values along the iterations
tempValues	vector of temperature values along the iterations
probaValues	vector of acceptance probability values along the iterations

**Author(s)**

G. Damblin & B. Iooss

**References**

- Damblin G., Couplet M., and Iooss B. (2013). Numerical studies of space filling designs: optimization of Latin Hypercube Samples and subprojection properties, *Journal of Simulation*, 7:276-289, 2013.
- M. Morris and J. Mitchell (1995) Exploratory designs for computational experiments. *Journal of Statistical Planning and Inference*, 43:381-402.
- R. Jin, W. Chen and A. Sudjianto (2005) An efficient algorithm for constructing optimal design of computer experiments. *Journal of Statistical Planning and Inference*, 134:268-287.
- Pronzato, L. and Muller, W. (2012). Design of computer experiments: space filling and beyond, *Statistics and Computing*, 22:681-701.

**See Also**

Latin Hypercube Sample ([lhsDesign](#)), discrepancy criteria ([discrepancyCriteria](#)), geometric criterion ([mindist](#), [phiP](#)), optimization ([maximinSA\\_LHS](#), [discrepESE\\_LHS](#), [discrepSA\\_LHS](#))

**Examples**

```
dimension <- 2
n <- 10
X <- lhsDesign(n, dimension)$design
Xopt <- maximinESE_LHS(X, T0=0.005*phiP(X), inner_it=100, J=50, it=2)
plot(Xopt$design)
plot(Xopt$critValues, type="l")
```

---

maximinSA_LHS	<i>Simulated annealing (SA) routine for Latin Hypercube Sample (LHS) optimization via phiP criteria</i>
---------------	---------------------------------------------------------------------------------------------------------

---

**Description**

The objective is to produce maximin LHS. SA is an efficient algorithm to produce space-filling designs.

**Usage**

```
maximinSA_LHS(design, T0=10, c=0.95, it=2000, p=50, profile="GEOM", Imax=100)
```

**Arguments**

design	a matrix (or a data.frame) corresponding to the design of experiments
T0	The initial temperature of the SA algorithm
c	A constant parameter regulating how the temperature goes down
it	The number of iterations
p	power required in phiP criterion
profile	The temperature down-profile, purely geometric called "GEOM", geometrical according to the Morris algorithm called "GEOM_MORRIS" or purely linear called "LINEAR"
Imax	A parameter given only if you choose the Morris down-profile. It adjusts the number of iterations without improvement before a new elementary perturbation

**Details**

This function implements a classical routine to produce optimized LHS. It is based on the work of Morris and Mitchell (1995). They have proposed a SA version for LHS optimization according to mindist criterion. Here, it has been adapted to the phiP criterion. It has been shown (Pronzato and Muller, 2012, Damblin et al., 2013) that optimizing phiP is more efficient to produce maximin designs than optimizing mindist. When  $p$  tends to infinity, optimizing a design with phi\_p is equivalent to optimizing a design with mindist.

**Value**

A list containing:

InitialDesign	the starting design
T0	the initial temperature of the SA algorithm
c	the constant parameter regulating how the temperature goes down
it	the number of iterations
p	power required in phiP criterion
profile	the temperature down-profile
Imax	The parameter given in the Morris down-profile
design	the matrix of the final design (maximin LHS)
critValues	vector of criterion values along the iterations
tempValues	vector of temperature values along the iterations
probaValues	vector of acceptance probability values along the iterations

**Author(s)**

G. Damblin & B. Iooss

**References**

- Damblin G., Couplet M., and Iooss B. (2013). Numerical studies of space filling designs: optimization of Latin Hypercube Samples and subprojection properties, *Journal of Simulation*, 7:276-289, 2013.
- M. Morris and J. Mitchell (1995) Exploratory designs for computational experiments. *Journal of Statistical Planning and Inference*, 43:381-402.
- R. Jin, W. Chen and A. Sudjianto (2005) An efficient algorithm for constructing optimal design of computer experiments. *Journal of Statistical Planning and Inference*, 134:268-287.
- Pronzato, L. and Muller, W. (2012). Design of computer experiments: space filling and beyond, *Statistics and Computing*, 22:681-701.

**See Also**

Latin Hypercube Sample ([lhsDesign](#)), discrepancy criteria ([discrepancyCriteria](#)), geometric criterion ([mindist](#), [phiP](#)), optimization ([discrepSA\\_LHS](#), [maximinESE\\_LHS](#), [discrepESE\\_LHS](#))

**Examples**

```
dimension <- 2
n <- 10
X <- lhsDesign(n ,dimension)$design
Xopt <- maximinSA_LHS(X, T0=10, c=0.99, it=2000)
plot(Xopt$design)
plot(Xopt$critValues, type="l")
plot(Xopt$tempValues, type="l")
```

```
## Not run:
  Xopt <- maximinSA_LHS(X, T0=10, c=0.99, it=1000, profile="GEOM_MORRIS")

## End(Not run)
```

---

 meshRatio

*MeshRatio measure*


---

### Description

The meshRatio criterion is the ratio between the maximum and the minimum distance between two points of the experimental design.

### Usage

```
meshRatio(design)
```

### Arguments

design a matrix (or a data.frame) representing the design of experiments in the unit cube  $[0,1]^d$ . If this last condition is not fulfilled, a transformation into  $[0,1]^d$  is applied before the computation of the criteria.

### Details

The meshRatio criterion is defined by

$$\text{meshRatio} = \frac{\max_{1 \leq i \leq n} \gamma_i}{\min_{1 \leq i \leq n} \gamma_i}$$

where  $\gamma_i$  denotes the minimal distance between the point  $x_i$  and the other points of the design.

Note that for a regular mesh, meshRatio=1.

### Value

A real number equal to the value of the meshRatio criterion for the design.

### Author(s)

J. Franco

### References

Gunzburger M. and Burkardt J. (2004), Uniformity measures for point samples in hypercubes, <https://people.sc.fsu.edu/~jburkardt/>.

### See Also

Other distance criteria like [meshRatio](#), [phiP](#) and [mindist](#).  
 Discrepancy measures provided by [discrepancyCriteria](#).

**Examples**

```
dimension <- 2
n <- 40
X <- matrix(runif(n*dimension), n, dimension)
meshRatio(X)
```

---

mindist

*Mindist measure*


---

**Description**

Compute the mindist criterion (also called maximin)

**Usage**

```
mindist(design)
```

**Arguments**

design            a matrix (or a data.frame) representing the design of experiments in the unit cube  $[0,1]^d$ . If this last condition is not fulfilled, a transformation into  $[0,1]^d$  is applied before the computation of the criteria.

**Details**

The mindist criterion is defined by

$$\text{mindist} = \min_{x_i \in X} (\gamma_i)$$

where  $\gamma_i$  is the minimal distance between the point  $x_i$  and the other points  $x_k$  of the design.

A higher value corresponds to a more regular scattering of design points.

**Value**

A real number equal to the value of the mindist criterion for the design.

**Author(s)**

J. Franco

**References**

Gunzburger M., Burkardt J. (2004), Uniformity measures for point samples in hypercubes, <https://people.sc.fsu.edu/~jburkardt/>.

Jonshon M.E., Moore L.M. and Ylvisaker D. (1990), Minmax and maximin distance designs, *J. of Statis. Planning and Inference*, 26, 131-148.

Chen V.C.P., Tsui K.L., Barton R.R. and Allen J.K. (2003), A review of design and modeling in computer experiments, *Handbook of Statistics*, 22, 231-261.

**See Also**

other distance criteria like [meshRatio](#) and [phiP](#), discrepancy measures provided by [discrepancyCriteria](#).

**Examples**

```
dimension <- 2
n <- 40
X <- matrix(runif(n*dimension), n, dimension)
mindist(X)
```

---

mstCriteria

*Deriving the MST criteria*

---

**Description**

Compute both the mean and the standard deviation of the Minimal Spanning Tree (MST)

**Usage**

```
mstCriteria(design, plot2d="FALSE")
```

**Arguments**

design	a matrix (or a data.frame) corresponding to the design of experiments.
plot2d	an argument for visualizing the mst of a 2d design

**Details**

In our context, a MST is a tree whose the sum of the lengths of the edges is minimal. Even if unicity does not hold, the overall length is stable. The mean and the standard deviation of the lengths of the edges are usually derived to analyze the geometric profile of the design. A large mean and a small standard deviation characterize a so-called quasi-periodic design.

**Value**

A list containing two components:

tree	a list containing the MST: each component of it contains a vector with all vertices which are connected with the experiment corresponding to the number of the components
stats	vector with both the mean and the standard deviation values of the lengths of the edges

**Author(s)**

G. Damblin & B. Iooss

## References

- Damblin G., Couplet M., and Iooss B. (2013). Numerical studies of space filling designs: optimization of Latin hypercube samples and subprojection properties, *Journal of Simulation*, 7:276-289, 2013.
- Dussert, C., Rasigni, G., Rasigni, M., and Palmari, J. (1986). Minimal spanning tree: A new approach for studying order and disorder. *Physical Review B*, 34(5):3528-3531.
- Franco J. (2008). Planification d'expériences numérique en phase exploratoire pour la simulation des phénomènes complexes, *PhD thesis, Ecole Nationale Supérieure des Mines de Saint Etienne*.
- Franco, J., Vasseur, O., Corre, B., and Sergent, M. (2009). Minimum spanning tree: A new approach to assess the quality of the design of computer experiments. *Chemometrics and Intelligent Laboratory Systems*, 97:164-169.
- Prim, R.C. (1957). Shortest connection networks and some generalizations, *in Bell System Technical Journal* 36:1389-1401.

## Examples

```
dimension <- 2
n <- 40
X <- matrix(runif(n*dimension), n, dimension)
mstCriteria(X, plot2d=TRUE)
```

---

nolhDesign

*Cioppa's Nearly Orthogonal Latin Hypercube Designs*


---

## Description

This function generates a NOLH design of dimension 2 to 29 and normalizes it to the selected range. The design is extracted from Cioppa's [NOLHdesigns](#) list.

## Usage

```
nolhDesign(dimension, range = c(0, 1))
```

## Arguments

dimension	number of input variables
range	the scale (min and max) of the inputs. Range (0, 0) and (1, 1) are special cases and call integer ranges $(-m, m)$ and $(0, 2m)$ . See the examples

## Value

A list with components:

n	the number of lines/experiments
dimension	the number of columns/input variables
design	the design of experiments



**Author(s)**

T.M. Cioppa for the designs. P. Kiener for the R code.

**See Also**

Cioppa's list [NOLHdesigns](#). Other NOLH and OLH designs: [nolhdrDesign](#), [olhDesign](#).

**Examples**

```
## Classical normalizations
nolhDesign(8, range = c(1, 1))
nolhDesign(8, range = c(0, 0))
nolhDesign(8, range = c(0, 1))
nolhDesign(8, range = c(-1, 1))

## Change the dimnames, adjust to range (-10, 10) and round to 2 digits
xDRDN(nolhDesign(8), letter = "T", dgts = 2, range = c(-10, 10))

## A list of designs
lapply(5:9, function(n) nolhDesign(n, range = c(-1, 1))$design)
```

---

NOLHdesigns

*List of Cioppa's Nearly Orthogonal Latin Hypercubes designs*

---

**Description**

A list of the NOLH designs for 2 to 29 input variables proposed by Cioppa in 2007. These designs combine a latin structure, orthogonality between the main terms and the interactions (+ squares) and reduced correlations between the interactions (+ squares).

This list combines the Excel spreadsheets published by Sanchez (see Source). It is used internally by the function [nolhDesign](#) which provides various normalizations.

**Usage**

NOLHdesigns

**Format**

A list of 5 matrices representing designs of experiments for 8 to 29 input variables:

```
nolh2_7: 2 to 7 input variables, 17 experiments.
nolh8_11: 8 to 11 input variables, 33 experiments.
nolh12_16: 12 to 16 input variables, 65 experiments.
nolh17_22: 17 to 22 input variables, 129 experiments.
nolh23_29: 23 to 29 input variables, 257 experiments.
```

**Author(s)**

T.M. Cioppa for the designs. P. Kiener for the R code.

**Source**

Sanchez, S. M. (2011). NOLHdesigns in Excel file. Available online at <https://nps.edu/web/seed/software-downloads/>

**References**

- Cioppa T.M., Lucas T.W. (2007). Efficient nearly orthogonal and space-filling Latin hypercubes. *Technometrics* 49, 45-55.
- Kleijnen, J.P.C., Sanchez S.M., T.W. Lucas and Cioppa T. M.. A user's guide to the brave new world of designing simulation experiments. *INFORMS Journal on Computing* 17(3): 263-289.
- Ye, K. Q. (1998). Orthogonal Latin hypercubes and their application in computer experiments. *J. Amer. Statist. Asso.* 93, 1430- 1439.

**See Also**

The main function `nolhDesign`. De Rainville's NOLH design list: [NOLHDRdesigns](#).

**Examples**

```
## data(NOLHdesigns)

## all matrices
names(NOLHdesigns)
lapply(NOLHDRdesigns, tail, 2)

## The first matrix/design
NOLHdesigns[["nolh2_7"]]
```

---

nolhdrDesign

*De Rainville's Nearly Orthogonal Latin Hypercube Designs*

---

**Description**

This function generates a NOLH design of dimension 2 to 29 and normalizes it to the selected range. From 2 to 7 input variables, the design is extracted from Cioppa's [NOLHdesigns](#) list and from 8 to 29 input variables it is extracted from De Rainville's [NOLHDRdesigns](#) list.

**Usage**

```
nolhdrDesign(dimension, range = c(0, 1))
```

**Arguments**

dimension	number of input variables
range	the scale (min and max) of the inputs. Range (0, 0) and (1, 1) are special cases and call integer ranges $(-m, m)$ and $(0, 2m)$ . See the examples

**Value**

A list with components:

n	the number of lines/experiments
dimension	the number of columns/input variables
design	the design of experiments

**Author(s)**

T.M. Cioppa and F.-M. De Rainville for the designs. P. Kiener for the R code.

**See Also**

De Rainville's list [NOLHDRdesigns](#). Other NOLH or OLH designs: [nolhDesign](#), [olhDesign](#).

**Examples**

```
## Classical normalizations
nolhdrDesign(8, range = c(1, 1))
nolhdrDesign(8, range = c(0, 1))
nolhdrDesign(8, range = c(0, 0))
nolhdrDesign(8, range = c(-1, 1))

## Change the dimnames, adjust to range (-10, 10) and round to 2 digits
xDRDN(nolhdrDesign(8), letter = "T", dgts = 2, range = c(-10, 10))

## A list of designs
lapply(5:9, function(n) nolhdrDesign(n, range = c(-1, 1))$design)
```

---

NOLHDRdesigns

*List of De Rainville's Nearly Orthogonal Latin Hypercubes designs*

---

**Description**

A list of the NOLH designs for 8 to 29 input variables proposed by De Rainville in 2012. These designs are said to be an improvement of Cioppa's NOLH designs as they have the same structure but better dispersion measures like the discrepancy.

This list combines the csv files published by De Rainville (see Source), centered and normalized to integer values. It is used internally by the function [nolhdrDesign](#) which provides various normalizations.

**Usage**

NOLHDRdesigns

**Format**

A list of 22 matrices representing designs of experiments for 8 to 29 input variables:

no1hdr08 to no1hdr11: 8, 9, 10, 11 input variables, 33 experiments.

no1hdr12 to no1hdr16: 12, 13, 14, 15, 16 input variables, 65 experiments.

no1hdr17 to no1hdr22: 17, 18, 19, 20, 21, 22 input variables, 129 experiments.

no1hdr23 to no1hdr29: 23, 24, 25, 26, 27, 28, 29 input variables, 257 experiments.

**Author(s)**

F.-M. De Rainville for the designs. P. Kiener for the R code.

**Source**

Main website: <http://qrand.gel.ulaval.ca/>

The python source code: <https://github.com/fmder/pynolh/>

The python package: <https://pypi.org/project/pynolh/>.

**References**

De Rainville F.-M., Gagne C., Teytaud O., Laurendeau D. (2012). Evolutionary optimization of low-discrepancy sequences. *ACM Transactions on Modeling and Computer Simulation (TOMACS)*, 22(2), 9.

Cioppa T.M., Lucas T.W. (2007). Efficient nearly orthogonal and space-filling Latin hypercubes. *Technometrics* 49, 45-55.

**See Also**

The main function `no1hdrDesign`. Cioppa's NOLH design list: [NOLHdesigns](#).

**Examples**

```
## data(NOLHDRdesigns)

## all matrices
names(NOLHDRdesigns)
lapply(NOLHDRdesigns, tail, 2)

## The first matrix/design
NOLHDRdesigns[["no1hdr08"]]
```

---

 OA131

 A 3D orthogonal array of strength 2
 

---

### Description

A 3-dimensional linear orthogonal array (OA) of strength 2 with 49 points. The design points are equally spaced into 2 dimensional coordinate planes. However by construction, such OAs satisfy a linear relation, here:  $x_1 + 3x_2 + x_3 = 0 \pmod{7}$ . As a consequence, the design points are contained in parallel planes orthogonal to (1,3,1). Actually, they are also contained in parallel planes orthogonal to other directions, as (2,-1,2) or (3,2,3), since the congruence relation leads to  $2x_1 - x_2 + 2x_3 = 0 \pmod{7}$  or  $3x_1 + 2x_2 + 3x_3 = 0 \pmod{7}$ . For instance, they are contained in 4 parallel planes orthogonal to (2,-1,2).

### Usage

```
data(OA131)
```

### Format

A data frame with 49 observations on the following 3 variables.

x1 first coordinate

x2 second coordinate

x3 third coordinate

### Source

Roustant O., Franco J., Carraro L., Jourdan A. (2010), A radial scanning statistic for selecting space-filling designs in computer experiments, MODA-9 proceedings.

### Examples

```
data(OA131)

# centering and reducing to [0,1]^3
OA <- (OA131 + 0.5)/7
pairs(OA, xlim=c(0,1), ylim=c(0,1))

## Not run:
library(lattice)
cloud(x3~x1+x2, data=OA, xlim=c(0,1), ylim=c(0,1), zlim=c(0,1),
      screen = list(z = 50, x = -70, y = 0))
## End(Not run)
```

---

OA131_scrambled	<i>A scrambled 3D orthogonal array of strength 2</i>
-----------------	------------------------------------------------------

---

**Description**

This design is obtained by adding a uniform noise to each coordinate of the orthogonal array OA131.

**Usage**

```
data(OA131_scrambled)
```

**Format**

A data frame with 49 observations on the following 3 variables.

```
x1 first coordinate
x2 second coordinate
x3 third coordinate
```

**Source**

Roustant O., Franco J., Carraro L., Jourdan A. (2010), A radial scanning statistic for selecting space-filling designs in computer experiments, MODA-9 proceedings.

**Examples**

```
data(OA131)
data(OA131_scrambled)

pairs(OA131, xlim=c(0,1), ylim=c(0,1))
pairs(OA131_scrambled, xlim=c(0,1), ylim=c(0,1))
```

---

olhDesign	<i>Nguyen's Orthogonal Latin Hypercube Designs</i>
-----------	----------------------------------------------------

---

**Description**

Generate the Orthogonal Latin Hypercube (OLH) designs proposed by Nguyen in 2008. These OLHs have a latin structure, an orthogonality between the main terms and the interactions (+ squares) and low correlations between the interactions (+ squares). Very large matrices can be obtained as the number of input variables and hence the number of lines is unconstrained. When the number of input variables is a power of 2, OLHs have  $d$  columns and  $n = 2d + 1$  lines (experiments). A vertical truncature is applied when the number of input variables is not a power of 2. Various normalizations can be applied.

**Usage**

```
olhDesign(dimension, range = c(0, 1))
```

**Arguments**

dimension	number of input variables
range	the scale (min and max) of the inputs. Ranges (0, 0) and (1, 1) are special cases and call integer ranges $(-d, d)$ and $(0, 2d)$ . See the examples

**Value**

A list with components:

n	the number of lines/experiments
dimension	the number of columns/input variables
design	the design of experiments

**Author(s)**

N.K. Nguyen for the algorithm. P. Kiener for the recursive R code.

**References**

Nguyen N.K. (2008) *A new class of orthogonal Latinhypercubes*, Statistics and Applications, Volume 6, issues 1 and 2, pp.119-123.

**See Also**

Cioppa's and De Rainville's NOLH designs: [nolhDesign](#), [nolhdrDesign](#).

**Examples**

```
## Classical normalizations
olhDesign(4, range = c(0, 0))
olhDesign(4, range = c(1, 1))
olhDesign(4, range = c(0, 1))
olhDesign(4, range = c(-1, 1))

## Change the dimnames, adjust to range (-10, 10) and round to 2 digits
xDRDN(olhDesign(4), letter = "T", dgts = 2, range = c(-10, 10))

## A list of designs
lapply(1:5, function(n) olhDesign(n, range = c(-1, 1))$design)
```

phiP

*phiP criterion***Description**

Compute the  $\phi_p$  criterion (strongly linked to mindist criterion)

**Usage**

```
phiP(design, p=50)
```

**Arguments**

`design` a matrix (or a data.frame) corresponding to the design of experiments.  
`p` the "p" in the Lp norm which is taken

**Details**

The  $\phi_p$  criterion is defined by the  $L_p$  norm of the sum of the inverses of the design inter-point euclidean distances:

$$\phi_p = \left[ \sum_{i,j=1 \dots N, i < j} d_{ij}^{-p} \right]^{\frac{1}{p}}$$

A higher value corresponds to a more regular scattering of design points.

When  $p$  tends to infinity, optimizing a design with  $\phi_p$  is equivalent to optimizing a design with mindist.

**Value**

A real number equal to the value of the  $\phi_p$  criterion for the design.

**Author(s)**

G. Damblin & B.Iooss

**References**

- Damblin G., Couplet M., and Iooss B. (2013). Numerical studies of sapce filling designs: optimization of Latin Hypercube Samples and subprojection properties, *Journal of Simulation*, 7:276-289, 2013.
- Fang K.-T., Li R. and Sudjianto A. (2006). Design and Modeling for Computer Experiments, *Chapman & Hall*.
- Pronzato, L. and Muller, W. (2012). Design of computer experiments: space filling and beyond, *Statistics and Computing*, 22:681-701.



**See Also**

geometric criterion ([mindist](#))

**Examples**

```
dimension <- 2
n <- 40
X <- matrix(runif(n*dimension), n, dimension)
phiP(X)
```

---

 rss2d

---

*2D graphical tool for defect detection of Space-Filling Designs.*


---

**Description**

For a 2-dimensional design, the 2D radial scanning statistic (RSS) scans angularly the domain. In each direction, it compares the distribution of projected points to their theoretical distribution under the assumption that all design points are drawn from uniform distribution. For a d-dimensional design, all pairs of dimensions are scanned. The RSS detects the defects of low discrepancy sequences or orthogonal arrays, and can be used for selecting space-filling designs.

**Usage**

```
rss2d(design, lower, upper, gof.test.type="greenwood",
      gof.test.stat=NULL, transform=NULL, n.angle=360, graphics=1,
      trace=TRUE, lines.lwd = 1, lines.lty = "dotted", ...)
```

**Arguments**

design	a matrix or data.frame containing the d-dimensional design of experiments. The row no. i contains the values of the d input variables corresponding to simulation no. i
lower	the domain lower boundaries.
upper	the domain upper boundaries.
gof.test.type	an optional character indicating the kind of statistical test to be used to test the goodness-of-fit of the design projections to their theoretical distribution. Several tests are available, see <a href="#">unif.test.statistic</a> . Default is "greenwood".
gof.test.stat	an optional number equal to the goodness-of-fit statistic at level 5%. Default is the modified test statistic for fully specified distribution (see details below).
transform	an optional character indicating what type of transformation should be applied before testing uniformity. Only one choice available "spacings", that lead to over-detection. Default - and recommended - is NULL.
n.angle	an optional number indicating the number of angles used. Default is 360 corresponding to a 0.5-degree discretization step. Note that the RSS curve is continuous.

<code>graphics</code>	an optional integer indicating whether a graph should be produced. If negative, no graph is produced. If superior to 2, the RSS curve only is plotted in the worst 2D coordinate subspace (corr. to the worst value of statistic). If 1 (default), the design is also added, with its projections onto the worst (oblique) axis.
<code>trace</code>	an optional boolean. Turn it to FALSE if you want no verbosity.
<code>lines.lwd</code>	optional number specifying the width of the straight lines involved in the graphical outputs (axis and projections)
<code>lines.lty</code>	optional character string specifying the type of the straight lines involved in the graphical outputs (axis and projections)
<code>...</code>	optional graphical parameters of plot function, to draw the RSS curve.

### Value

a list with components:

<code>global.stat</code>	a matrix containing the values of the global statistic (equal to the maximum of statistic values over the RSS curve) for all pairs of dimensions.
<code>worst.case</code>	the worst pair of dimensions, that is the one that gives the worst value of <code>global.stat</code> .
<code>worst.dir</code>	the worst direction, that is the one that gives the worst value of the global statistic in the coordinate plane defined by <code>worst.case</code> .
<code>stat</code>	a vector of length <code>n.angle</code> containing the statistic values for each angle, in the coordinate plane defined by <code>worst.case</code> .
<code>angle</code>	a vector of length <code>n.angle</code> containing the corresponding angles used.
<code>curve</code>	a $(2*n.angle) \times 2$ matrix containing the discretized RSS curve.
<code>gof.test.stat</code>	the threshold at significance level 0.05 for the specified goodness-of-fit statistic. It is equal to the radius of the circle superimposed on the RSS figure.

### Author(s)

O. Roustant

### References

- Roustant O., Franco J., Carraro L., Jourdan A. (2010), A radial scanning statistic for selecting space-filling designs in computer experiments, MODA-9 proceedings.
- D Agostino R.B., Stephens M.A. (1986), Goodness-of-fit techniques, CRC Press, New York.

### See Also

[unif.test.statistic](#), [unif.test.quantile](#), [rss3d](#)

## Examples

```
## Detection of defects of Sobol designs

## requires randtoolbox package
library(randtoolbox)

## In 2D
rss <- rss2d(design=sobol(n=20, dim=2), lower=c(0,0), upper=c(1,1),
             type="l", col="red")

## In 8D
## All pairs of dimensions are tried to detect the worst defect
## (according to the specified goodness-of-fit statistic).
d <- 8
n <- 10*d
rss <- rss2d(design=sobol(n=n, dim=d), lower=rep(0,d), upper=rep(1,d),
             type="l", col="red")

## Avoid this defect with scrambling?
## 1. Faure-Tezuka scrambling (type "?sobol" for more details and options)
rss <- rss2d(design=sobol(n=n, dim=d, scrambling=2), lower=rep(0,d), upper=rep(1,d),
             type="l", col="red")
## 2. Owen scrambling
rss <- rss2d(design=sobol(n=n, dim=d, scrambling=1), lower=rep(0,d), upper=rep(1,d),
             type="l", col="red")
```

---

 rss3d

---

*3D graphical tool for defect detection of Space-Filling Designs.*


---

## Description

For a 3-dimensional design, the 3D radial scanning statistic (RSS) scans angularly the domain. In each direction, it compares the distribution of projected points to their theoretical distribution under the assumption that all design points are drawn from uniform distribution. For a d-dimensional design, all triplets of dimensions are scanned. The RSS detects the defects of low discrepancy sequences or orthogonal arrays, and can be used for selecting space-filling designs.

## Usage

```
rss3d(design, lower, upper, gof.test.type = "greenwood",
      gof.test.stat = NULL, transform = NULL, n.angle = 60,
      graphics = 1, trace = TRUE)
```

## Arguments

design	a matrix or data.frame containing the d-dimensional design of experiments. The row no. i contains the values of the d input variables corresponding to simulation no. i
--------	-------------------------------------------------------------------------------------------------------------------------------------------------------------------------

lower	the domain lower boundaries.
upper	the domain upper boundaries.
gof.test.type	an optional character indicating the kind of statistical test to be used to test the goodness-of-fit of the design projections to their theoretical distribution. Several tests are available, see <code>unif.test.statistic</code> . Default is "greenwood".
gof.test.stat	an optional number equal to the goodness-of-fit statistic at level 5%. Default is the modified test statistic for fully specified distribution (see details below).
transform	an optional character indicating what type of transformation should be applied before testing uniformity. Only one choice available "spacings", that lead to over-detection. Default - and recommended - is NULL.
n.angle	an optional number indicating the number of angles used. Default is 60 corresponding to a 3-degree discretization step. Note that the RSS surface is continuous.
graphics	an optional integer indicating whether a graph should be produced. If negative, no graph is produced. Otherwise (default), the design is plotted in the worst 3D coordinate subspace (corr. to the worst value of statistic), with its projections onto the worst (oblique) axis.
trace	an optional boolean. Turn it to FALSE if you want no verbosity.

### Details

The RSS surface is continuous. However for computational purposes, a discretization is used. The default discretization step is tunable with `n.angle`.

### Value

a list with components:

<code>global.stat</code>	an array containing the values of the global statistic (equal to the maximum of statistic values over the RSS surface) for all triplets of dimensions.
<code>print.out</code>	the same as <code>global.stat</code> , but with a user-friendly printing.
<code>worst.case</code>	the worst triplet of dimensions, that is the one that gives the worst value of <code>global.stat</code> .
<code>worst.dir</code>	the worst direction, that is the one that gives the worst value of the statistic in the coordinate 3D subspace defined by <code>worst.case</code> .
<code>stat</code>	a matrix of size <code>n.angle*n.angle</code> containing the statistic values for each angles (spherical coordinates).
<code>angle</code>	a matrix of size <code>n.angle*n.angle</code> containing the corresponding angles used (spherical coordinates).
<code>gof.test.stat</code>	the threshold at significance level 0.05 for the specified goodness-of-fit statistic.

### Author(s)

O. Roustant

## References

Roustant O., Franco J., Carraro L., Jourdan A. (2010), A radial scanning statistic for selecting space-filling designs in computer experiments, MODA-9 proceedings.

D Agostino R.B., Stephens M.A. (1986), Goodness-of-fit techniques, CRC Press, New York.

## See Also

[unif.test.statistic](#), [unif.test.quantile](#), [rss2d](#)

## Examples

```
## An orthogonal array in 3D
data(OA131)

## centering the design points of this 7-levels design
OA <- (OA131 + 0.5)/7

## 2D projections onto coordinate axis
pairs(OA, xlim=c(0,1), ylim=c(0,1))
## Now let us look at the 3D properties with the 3D RSS (requires the rgl package)
rss <- rss3d(OA, lower=c(0,0,0), upper=c(1,1,1))
## The worst direction detected is nearly proportional to (2,-1,2)
## (type "?OA131" for explanations about this linear orthogonal array)
print(rss$worst.dir)

## Now, scramble this design
## X <- (OA131 + matrix(runif(49*3, 49, 3)))/7
## or load the design obtained this way
data(OA131_scrambled)
OA2 <- OA131_scrambled

## No feature is detected by the 2D RSS:
rss <- rss2d(OA2, lower=c(0,0,0), upper=c(1,1,1))
## 4 clusters are detected by the 3D RSS:
rss <- rss3d(OA2, lower=c(0,0,0), upper=c(1,1,1))

## Defect detection of 8D Sobol sequences
## All triplets of dimensions are tried to detect the worst defect
## (according to the specified goodness-of-fit statistic).
## requires randtoolbox library to generate the Sobol sequence
## Not run:
library(randtoolbox)
d <- 8
n <- 10*d
rss <- rss3d(design=sobol(n=n, dim=d), lower=rep(0,d), upper=rep(1,d))
## End(Not run)
```

---

`runif.faure`*Low discrepancy sequence : Faure*

---

### Description

Generate a Faure sequence with  $n$  experiments in  $[0,1]^d$ .

### Usage

```
runif.faure(n, dimension)
```

### Arguments

<code>n</code>	the number of experiments
<code>dimension</code>	the number of variables (<100)

### Details

A quasirandom or low discrepancy sequence, such as the Faure, Halton, Hammersley, Niederreiter or Sobol sequences, is "less random" than a pseudorandom number sequence, but more useful for such tasks as approximation of integrals in higher dimensions, and in global optimization. This is because low discrepancy sequences tend to sample space "more uniformly" than random numbers. see **randtoolbox** or **fOptions** packages for other low discrepancy sequences.

### Value

`runif.halton` returns a list containing all the input arguments detailed before, plus the following component:

<code>design</code>	the design of experiments
---------------------	---------------------------

### Author(s)

J. Franco

### References

Faure H. (1982), Discrepance de suites associees a un systeme de numeration (en dimension  $s$ ), *Acta Arith.*, 41, 337-351

### Examples

```
f <- runif.faure(20,2)
plot(f$design, xlim=c(0,1), ylim=c(0,1))
xDRDN(f, letter="T", dgts=2, range=c(-10, 10))
```

---

scaleDesign                      *Scale a Design*

---

### Description

This function scales the values of the design points to values comprised in [0,1]. The scaling can be made by the Rosenblatt transformation (uniformization by applying the empirical cumulative distribution function) or by translating the design from maximum and minimum values (given for each variable).

### Usage

```
scaleDesign(design, min=NULL, max=NULL, uniformize=FALSE)
```

### Arguments

design	a matrix (or a data.frame) corresponding to the design of experiments to scale
min	the vector of minimal bounds of each design variable. If not given, the minimal value of each variable is taken
max	the vector of maximal bounds of each design variable. If not given, the maximal value of each variable is taken
uniformize	boolean: TRUE to use the Rosenblatt transformation (the min and max vectors are useless in this case). If FALSE (default value), the translation from max and min values is applied

### Value

A list containing:

design	the scaled design
min	the vector of minimal bounds that has been used
max	the vector of maximal bounds that has been used
uniformize	the value of this boolean argument
InitialDesign	the starting design

### Author(s)

B. Iooss

### Examples

```
d <- 2
n <- 100
x <- matrix(rnorm(d*n), ncol=d)
xscale1 <- scaleDesign(x, uniformize=FALSE)
xscale2 <- scaleDesign(x, uniformize=TRUE)
par(mfrow=c(1,2))
plot(xscale1$design) ; plot(xscale2$design)
```

---

straussDesign                      *Designs based on Strauss process*

---

### Description

Space-Filling Designs based on Strauss process

### Usage

```
straussDesign(n,dimension, RND, alpha=0.5, repulsion=0.001, NMC=1000,
              constraints1D=0, repulsion1D=0.0001, seed=NULL)
```

### Arguments

n	the number of experiments
dimension	the number of input variables
RND	a real number which represents the radius of interaction
alpha	the potential power (default, fixed at 0.5)
repulsion	the repulsion parameter in the unit cube (gamma)
NMC	the number of McMC iterations (this number must be large to converge)
constraints1D	1 to impose 1D projection constraints, 0 otherwise
repulsion1D	the repulsion parameter in 1D
seed	seed for the uniform generation of number

### Details

Strauss designs are Space-Filling designs initially defined from Strauss process:

$$\pi(X) = k\gamma^{s(X)}$$

where  $s(X)$  is the number of pairs of points  $(x^i, x^j)$  of the design  $X = (x^1, \dots, x^n)$  that are separated by a distance no greater than the radius of interaction RND,  $k$  is the normalizing constant and  $\gamma$  is the repulsion parameter. This distribution corresponds to the particular case  $\alpha=0$ .

For the general case, a stochastic simulation is used to construct a Markov chain which converges to a spatial density of points  $\pi(X)$  described by the Strauss-Gibbs potential. In practice, the Metropolis-Hastings algorithm is implemented to simulate a distribution of points which converges to the stationary law:

$$\pi(X) \propto \exp(-U(X))$$

with a potential  $U$  defined by:

$$U(X) = \beta \sum_{1 \leq i < j \leq n} \varphi(\|x^i - x^j\|)$$

where  $\beta = -\ln \gamma$ ,  $\varphi(h) = (1 - \frac{h}{RND})^\alpha$  if  $h \leq RND$  and 0 otherwise.



The input parameters of `straussDesign` function can be interpreted as follows:

- `RND` is used to compute the number of pairs of points of the design separated by a distance no more than `RND`. A point is said "in interaction" with another if the spheres of radius `RND/2` centered on these points intersect.
- `alpha` is the potential power  $\alpha$ . The case `alpha=0` corresponds to Strauss process (0-1 potential).
- `repulsion` is equal to the  $\gamma$  parameter of the Strauss process. Note that  $\gamma$  belongs to  $]0,1[$ .
- `constraints1D` allows to specify some constraints into the margin. If `constraints1D==1`, two repulsion parameters are needed: one for the all space (`repulsion`) and the other for the 1D projection (`repulsion1D`). Default values are `repulsion=0.001` and `repulsion1D=0.001`. Note that the value of the radius of interaction in the one-dimensional axis is not an input parameter and is automatically fixed at  $0.75/n$ .

### Value

A list containing:

<code>n</code>	the number of experiments
<code>dimension</code>	the number $d$ of variables
<code>design_init</code>	the initial distribution of $n$ points $[0, 1]^d$
<code>radius</code>	the radius of interaction
<code>alpha</code>	the potential power $\alpha$
<code>repulsion</code>	the repulsion parameter $\gamma$
<code>NMC</code>	the number of iterations MCMC
<code>constraints1D</code>	an integer indicating if constraints on the factorial axis are imposed. If its value is different from zero, a component <code>repulsion1D</code> containing the value of the repulsion parameter $\gamma$ in dimension 1 is added at the list.
<code>design</code>	the design of experiments in $[0,1]^d$
<code>seed</code>	the seed corresponding to the design

### Author(s)

J. Franco

### References

J. Franco, X. Bay, B. Corre and D. Dupuy (2008) Planification d'expériences numériques à partir du processus ponctuel de Strauss, <https://hal.science/hal-00260701/fr/>.

### Examples

```
## Strauss-Gibbs designs in dimension 2 (n=20 points)
S1 <- straussDesign(n=20, dimension=2, RND=0.2)
plot(S1$design, xlim=c(0,1), ylim=c(0,1))
theta <- seq(0,2*pi, by=2*pi/(100 - 1))
for(i in 1:S1$n){
  lines(S1$design[i,1]+S1$radius/2*cos(theta),
```

```

        S1$design[i,2]+S1$radius/2*sin(theta), col='red')
    }

## 2D-Strauss design
S2 <- straussDesign(n=20, dimension=2, RND=0.2, NMC=200,
                   constraints1D=0, alpha=0, repulsion=0.01)
plot(S2$design,xlim=c(0,1),ylim=c(0,1))

## 2D-Strauss designs with constraints on the axis
S3 <- straussDesign(n=20, dimension=2, RND=0.18, NMC=200,
                   constraints1D=1, alpha=0.5, repulsion=0.1, repulsion1D=0.01)
plot(S3$design, xlim=c(0,1),ylim=c(0,1))
rug(S3$design[,1], side=1)
rug(S3$design[,2], side=2)

## Change the dimnames, adjust to range (-10, 10) and round to 2 digits
xDRDN(S3, letter="T", dgts=2, range=c(-10, 10))

```

---

unif.test.quantile      *Quantile of some uniformity tests*

---

## Description

Computes the quantile of a uniformity test at a given significance level (see available tests and levels below).

## Usage

```
unif.test.quantile(type, n, alpha)
```

## Arguments

type	a character indicating which test is used. The choices are the following: "greenwood", "qm" (for Quesenberry-Miller), "ks" (Kolmogorov-Smirnov), "cvm" (Cramer-Von Mises) and "V" (D+ + D- from Kolmogorov-Smirnov).
n	an integer equal to the sample size.
alpha	a real number equal to significance level. At present stage, only four values are available: 0.1, 0.05, 0.025 and 0.01.

## Details

Modified statistics are used. For  $\alpha = 0.05$ , the quantile is (see D Agostino and Stephens, 1986, section 4.4.):  $1.358/(\sqrt{n}) + 0.12 + 0.11/\sqrt{n}$  for Kolmogorov-Smirnov and  $0.461/(1+1/n) + 0.4/n - 0.6/n^2$  for Cramer-von Mises. When the design size is  $< 20$ , the corrected value seems to be a good approximation, but the non asymptotical value should be preferred.

**Value**

A real number equal to the quantile of the specified test at significance level alpha for n observations.

**Author(s)**

O. Roustant

**References**

D Agostino R.B., Stephens M.A. (1986), Goodness-of-fit techniques, CRC Press, New York.

**See Also**

[unif.test.statistic](#), [rss2d](#), [rss3d](#)

---

`unif.test.statistic`     *Statistic of some uniformity tests*

---

**Description**

Computes the statistic of a uniformity test (see available tests below).

**Usage**

```
unif.test.statistic(x, type, transform=NULL)
```

**Arguments**

<code>x</code>	a vector containing the sample values.
<code>type</code>	a character indicating which test is used. The choices are the following: "greenwood", "qm" (for Quesenberry-Miller), "ks" (Kolmogorov-Smirnov), "cvm" (Cramer-Von Mises) and "V" (D+ + D- from Kolmogorov-Smirnov).
<code>transform</code>	an optional character indicating what type of transformation should be applied before testing uniformity. Default is NULL.

**Value**

A real number equal to the statistic of the specified test.

**Author(s)**

O. Roustant

**References**

D Agostino R.B., Stephens M.A. (1986), Goodness-of-fit techniques, CRC Press, New York.

**See Also**

[unif.test.quantile, rss2d](#)

---

unscaleDesign

*Unscale a Design*

---

**Description**

This function unscales the values of a scaled design (values in [0,1]). The unscaling can be made by the inverse Rosenblatt transformation (by applying the empirical quantile function given by another design) or by translating the design from maximum and minimum values (given for each variable).

**Usage**

```
unscaleDesign(design, min=NULL, max=NULL, uniformize=FALSE, InitialDesign=NULL)
```

**Arguments**

design	a matrix (or a data.frame) corresponding to the design of experiments to unscale
min	the vector of minimal bounds of each design variable
max	the vector of maximal bounds of each design variable
uniformize	boolean: TRUE to use the inverse Rosenblatt transformation (the min and max vectors are useless in this case). If FALSE (default value), the translation from max and min values is applied
InitialDesign	If the inverse Rosenblatt transformation is applied (uniformize = TRUE): a matrix (or a data.frame) corresponding to the design which gives the empirical quantiles

**Value**

A list containing:

design	the unscaled design
min	the vector of minimal bounds that has been used
max	the vector of maximal bounds that has been used
uniformize	the value of this boolean argument

**Author(s)**

B. Iooss

**Examples**

```

d <- 2
n <- 100
x <- matrix(rnorm(d*n), ncol=d)
xscale <- scaleDesign(x, uniformize=TRUE)
xunscale1 <- unscaleDesign(xscale$design, uniformize=TRUE, InitialDesign=x)
xunscale2 <- unscaleDesign(xscale$design,
min=c(min(x[,1]), min(x[,2])), max = c(max(x[,1]), max(x[,2])))
par(mfrow=c(2,2))
plot(x) ; plot(xscale$design)
plot(xunscale1$design) ; plot(xunscale2$design)

```

wspDesign

*WSP algorithm***Description**

The WSP (Wooton, Sergeant, Phan-Tan-Luu) algorithm is an iterative algorithm based on suppression of some experiments from an initial design in each step. WSP leads to a space filling design

**Usage**

```
wspDesign(design, dmin, init = "center")
```

**Arguments**

design	a matrix (or a data.frame) corresponding to the design of experiments
dmin	a minimum bound for mindist value of the final design
init	defines the initialization point (input coordinates) of the algorithm: "center" (default value) takes the central point of the domain "random" takes a random point inside the domain

**Details**

WSP enables to create a design  $D$  which is such that  $\text{mindist}(D) > \text{dmin}$ . However, it cannot assess the number of experiments. Similarly to `strausDesign` function, WSP is a powerful algorithm to construct space filling designs in high dimension

**Value**

A list containing:

InitialDesign	the starting design
dmin	minimum bound for mindist value of the final design
design	the matrix of the final design
ResidualDesign	the matrix of the residual design (points of InitialDesign not in design)

**Author(s)**

G. Damblin & B. Iooss

**References**

J. Santiago, M. Claeys-Bruno, M.Sergent (2012). Construction of space filling designs using WSP algorithm for high dimensional spaces, *Chenometrics and Intelligent Laboratory Systems*, 113:26-31.

**Examples**

```
dimension <- 2
n <- 100
X <- matrix(runif(n*dimension), n, dimension)
m <- wspDesign(X, 0.1)
plot(m$design)
xDRDN(m, letter = "T", dgts = 2, range = c(-10, 10))
```

---

xDRDN

---

*Extract a Design and Give it a Range and Dimnames*


---

**Description**

Extract a design contained in a list (i.e. with a *design* item), adjust the range, give it dimnames and finally round the values to a certain number of digits. Colnames will look like (A, B, C), (X1, X2, X3), (X01, X02, X03), (X001, X002, X003).

**Usage**

```
xDRDN(obj, width = 1, letter = "X", dgts = NULL, range = NULL)
```

**Arguments**

obj	a list that contains a design item. Matrix or data.frame are also accepted
width	the digit width in colnames (to write for instance X1, X01, X001). If 0, colnames are filled with capital and small letters (without letters I and i) up to 50 columns
letter	the generic letter used in colnames
dgts	the number of digits to which the design is rounded
range	a vector c(min, max) to adjust the range of the design. The default NULL keeps the original range. Special ranges c(0, 0) and c(1, 1) are not accepted

**Value**

A rounded matrix or a data.frame with appropriate dimnames and an adjusted range.

**Examples**

```
xDRDN(lhsDesign(5, 12))  
xDRDN(lhsDesign(5, 12), width = 2, letter = "V", dgts = 2, range = c(-10, 10))  
head(xDRDN(olhDesign(50, range = c(1,1)), width = 0, letter = "Z"), 3)  
head(xDRDN(olhDesign(51, range = c(1,1)), width = 0, letter = "Z"), 3)
```

# Index

## \* datasets

NOLHdesigns, 25  
NOLHDRdesigns, 27  
OA131, 29  
OA131\_scrambled, 30

## \* design

coverage, 5  
discrepancyCriteria, 6  
discrepESE\_LHS, 8  
discrepSA\_LHS, 9  
dmaxDesign, 11  
factDesign, 13  
faureprimeDesign, 14  
lhsDesign, 16  
maximinESE\_LHS, 17  
maximinSA\_LHS, 19  
meshRatio, 21  
mindist, 22  
mstCriteria, 23  
nolhDesign, 24  
nolhdrDesign, 26  
olhDesign, 30  
phiP, 32  
rss2d, 33  
rss3d, 35  
runif.faure, 38  
straussDesign, 40  
unif.test.quantile, 42  
unif.test.statistic, 43  
wspDesign, 45

## \* package

DiceDesign-package, 2

coverage, 5, 7

DiceDesign (DiceDesign-package), 2  
DiceDesign-package, 2  
discrepancyCriteria, 5, 6, 9, 11, 19–21, 23  
discrepESE\_LHS, 8, 11, 17, 19, 20  
discrepSA\_LHS, 9, 9, 17, 19, 20

dmaxDesign, 11

factDesign, 13  
faureprimeDesign, 14

lhsDesign, 9, 11, 16, 19, 20

maximinESE\_LHS, 9, 11, 17, 17, 20  
maximinSA\_LHS, 9, 11, 17, 19, 19  
meshRatio, 5, 7, 21, 21, 23  
mindist, 5, 7, 9, 11, 19–21, 22, 33  
mstCriteria, 23

nolhDesign, 24, 25–27, 31  
NOLHdesigns, 24, 25, 25, 26, 28  
nolhdrDesign, 25, 26, 27, 28, 31  
NOLHDRdesigns, 26, 27, 27

OA131, 29  
OA131\_scrambled, 30  
olhDesign, 25, 27, 30

phiP, 5, 7, 9, 11, 19–21, 23, 32

rss2d, 33, 37, 43, 44  
rss3d, 34, 35, 43  
runif.faure, 14, 38

scaleDesign, 39  
straussDesign, 40

unif.test.quantile, 34, 37, 42, 44  
unif.test.statistic, 33, 34, 36, 37, 43, 43  
unscaleDesign, 44

wspDesign, 45

xDRDN, 46